Velocity calibration and wavefield decomposition for walkover VSP data

Markus von Steht and Jürgen Mann

Wave Inversion Technology Consortium Geophysical Institute, University of Karlsruhe (TH)



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Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



Overview

Theory

CRS approach for VSP geometry FO CRS traveltime approximation Calibration method

Data example

Survey description Velocity calibration Wavefield decomposition

Conclusions & outlook

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



◆□ ▶ ▲□ ▶ 少々で

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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



▲□▶ ▲□▶ ろくで

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 second order approximation based on paraxial ray-theory Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



Finite-offset (FO) 2D CRS stack theory initially introduced for surface seismic (Zhang et al., 2001)

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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



VSP measurement configuration



S and G are the positions of $\vec{x_S}$ and $\vec{x_G}$, respectively

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



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$$\begin{split} \tau_{\text{hyp}}^2 &= \left(\begin{array}{c} \tau_0 + \frac{\sin\beta_S}{v_S} \Delta x_S - \frac{\cos\beta_S}{v_S} \Delta z_S + \frac{\sin\beta_G}{v_G} \Delta x_G - \frac{\cos\beta_G}{v_G} \Delta z_G \end{array} \right)^2 \\ &+ \tau_0 \ AB^{-1} \ \left(\Delta x_S - \Delta z_S \tan\beta_S \right)^2 \\ &+ \tau_0 \ DB^{-1} \ \left(\Delta x_G - \Delta z_G \tan\beta_G \right)^2 \\ &- 2 \ \tau_0 \ B^{-1} \ \left(\Delta x_S - \Delta z_S \tan\beta_S \right) \left(\Delta x_G - \Delta z_G \tan\beta_G \right). \end{split}$$

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$$\tau_0$$
: traveltime of central FO ray

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- τ_0 : traveltime of central FO ray
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- ▶ β_S , β_G : emergence angles of central ray
- ► DB⁻¹, AB⁻¹, B⁻¹: composites of elements of ray-propagator matrix

A look at multi-coverage walkover data

Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



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A look at multi-coverage walkover data



Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



・ロト ・日 ・ うへで

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



▲□▶ ▲□▶ ろくで

Stacking parameters are converted to wavefield attributes by using tuned velocities.

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



◆□ ▶ ▲□ ▶ 少々で

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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Assumption:

Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Assumption:

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 - → length of slowness vector $|\vec{p}|$ independent of incidence angle

Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



Calibration strategy

Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



・ロマ ・日マ うくで
VSP data provides only one slowness component:

Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



・ロマ ・日マ うくで

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



・ロマ ・日マ うくで

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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



・ロマ ・日マ うくで

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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 - for each *G*, search maximum of $p_t(\vec{x}_S, \vec{x}_G = \text{const})$
 - ► searched-for velocity $v(\vec{x}_G) = \max \{p_t(\vec{x}_S; \vec{x}_G)\}^{-1}$

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



 surface	Velocity calibration and wavefield decomposition
well	M. von Steht & J. Manr
	Overview
	Theory CRS stack for VSP FO CRS-Operator Calibration method
	Data example Survey description Velocity calibration Decomposition
	Conclusions & outlook
]	

	surface	Velocity calibration and wavefield
	well	decomposition M. von Steht & J. Mann
		Overview
		Theory CRS stack for VSP FO CRS-Operator Calibration method
downgoing ray		Data example Survey description Velocity calibration Decomposition
		Conclusions & outlook



	surface	Velocity calibration and wavefield decomposition
	well	M. von Steht & J. Man
\mathbf{X}		Overview
		Theory CRS stack for VSP FO CRS-Operator Calibration method
		Data example Survey description Velocity calibration Decomposition
		Conclusions & outlool

	surface	Velocity calibration and wavefield decomposition
$\langle \rangle$	well	M. von Steht & J. Mai
\backslash		Overview
		Theory CRS stack for VSP FO CRS-Operator Calibration method
		Data example Survey description Velocity calibration Decomposition
		Conclusions & outloc
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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



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separate calibration for P- and S-waves

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



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- separate calibration for P- and S-waves
- velocity v_G is property of receiver position

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



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 applicable to also calibrate *reflected* waves

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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 - emergence angles
 - wavefront curvatures
- suited for

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



- separate calibration for P- and S-waves
- velocity v_G is property of receiver position
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 - wavefront curvatures
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Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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 - wavefront curvatures
- suited for
 - wavefield decomposition by data example

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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 - emergence angles
 - wavefront curvatures
- suited for
 - wavefield decomposition by data example
 - redatuming

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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 - emergence angles
 - wavefront curvatures
- suited for

 - redatuming
 - inversion

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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 - wavefront curvatures
- suited for
 - wavefield decomposition by data example
 - redatuming
 - inversion
- strategy also suited for deviated wells

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Survey description Velocity calibration Decomposition

Conclusions & outlook



◆□ ▶ ▲□ ▶ 少々で



P-wave velocity [km/s]

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Survey description Velocity calibration Decomposition

Conclusions & outlook



▲□▼ ▲□▼ ろくで

Modeling:

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Survey description Velocity calibration Decomposition

Conclusions & outlook



◆□ ▶ ▲□ ▶ 少々で

Modeling:

wavefront construction method

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Survey description Velocity calibration Decomposition

Conclusions & outlook



▲□▶ ▲□▶ 少々で
Modeling:

- wavefront construction method
- direct P, reflected PP & SS, converted PS

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Survey description Velocity calibration Decomposition



Modeling:

- wavefront construction method
- direct P, reflected PP & SS, converted PS
- 3D wave propagation

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example <u>Surv</u>ey description

Velocity calibration Decomposition



Modeling:

- wavefront construction method
- direct P, reflected PP & SS, converted PS
- 3D wave propagation
- two walkover lines, 100 shots each

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example

Survey description Velocity calibration Decomposition



Modeling:

- wavefront construction method
- direct P, reflected PP & SS, converted PS
- 3D wave propagation
- two walkover lines, 100 shots each
- 40 three-component receiver levels

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example

Survey description Velocity calibration Decomposition



Modeling:

- wavefront construction method
- direct P, reflected PP & SS, converted PS
- 3D wave propagation
- two walkover lines, 100 shots each
- 40 three-component receiver levels
- 2D approach sufficiently accurate for calibration

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example

Survey description Velocity calibration Decomposition



Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Survey description Velocity calibration Decomposition

Conclusions & outlook



◆□ ▶ ▲□ ▶ 少々で

convenient CRS parameter: emergence angle

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Survey description Velocity calibration Decomposition

Conclusions & outlook



▲□▶ ▲□▶ ろくで

convenient CRS parameter: emergence angle

 \blacktriangleright tangency \equiv zero angle

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Survey description Velocity calibration Decomposition

Conclusions & outlook



・ロマ ・日マ うくで

convenient CRS parameter: emergence angle

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Expected behavior:

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Survey description Velocity calibration Decomposition



convenient CRS parameter: emergence angle

 \blacktriangleright tangency \equiv zero angle

Expected behavior:

over-estimated velocity

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Survey description Velocity calibration Decomposition



convenient CRS parameter: emergence angle

 \blacktriangleright tangency \equiv zero angle

Expected behavior:

 over-estimated velocity zero angle smeared over large offset range Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Survey description Velocity calibration Decomposition



convenient CRS parameter: emergence angle

 \blacktriangleright tangency \equiv zero angle

Expected behavior:

- over-estimated velocity zero angle smeared over large offset range
- under-estimated velocity

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example

Survey description Velocity calibration Decomposition



convenient CRS parameter: emergence angle

 \blacktriangleright tangency \equiv zero angle

Expected behavior:

- over-estimated velocity zero angle smeared over large offset range
- under-estimated velocity zero angle never occurs

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example

Survey description Velocity calibration Decomposition



convenient CRS parameter: emergence angle

 \blacktriangleright tangency \equiv zero angle

Expected behavior:

- over-estimated velocity zero angle smeared over large offset range
- under-estimated velocity zero angle never occurs
- correct velocity

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example

Survey description Velocity calibration Decomposition



convenient CRS parameter: emergence angle

 \blacktriangleright tangency \equiv zero angle

Expected behavior:

- over-estimated velocity zero angle smeared over large offset range
- under-estimated velocity zero angle never occurs
- correct velocity well-localized minimum at zero angle

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example

Survey description Velocity calibration Decomposition



Calibration using checkshot inversion

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



・ロマ ・日マ うくで

Calibration using checkshot inversion



Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



▲□▶ ▲□▶ 少々で

Calibration with initial model



Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



▲□▶ ▲□▶ 少々で

Calibration with corrected model



Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



・ロマ ・日マ うくで

Forward-modeled angles



Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



・ロマ ・日マ うくで

1D velocity curves along well

Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



▲□▶ ▲□▶ ろくで

1D velocity curves along well



Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



▲□▼ ▲□▼ ろくで

CRS-based wavefield decomposition

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



◆□ ▶ ▲□ ▶ 少々で

CRS-based wavefield decomposition S



Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



▲□▼ ▲□▼ ろく(?)

CRS-based wavefield decomposition



Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



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CRS-based wavefield decomposition S



Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



▲□▶ ▲母▼ 釣∢?



Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory

CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description

Velocity calibration Decomposition





Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory

CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



Five CS gathers after decomposition



Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



Five CS gathers after decomposition



Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



▲□▶ ▲母 ▶ 釣へで

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



・ロマ ・日マ うくで

Calibration of CRS attributes

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



・ロマ ・日マ うくで

Calibration of CRS attributes

high sensitivity to inaccurate velocity

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



▲□▶ ▲母▼ 少々で

Calibration of CRS attributes

- high sensitivity to inaccurate velocity
- simple criterion to determine tuned velocities

Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



Calibration of CRS attributes

- high sensitivity to inaccurate velocity
- simple criterion to determine tuned velocities
- readily applicable to 3D data and deviated wells

Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



Calibration of CRS attributes

- high sensitivity to inaccurate velocity
- simple criterion to determine tuned velocities
- readily applicable to 3D data and deviated wells
- reliable geometrical CRS attributes for

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition


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 - wavefield decomposition

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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 - wavefield decomposition
 - redatuming

Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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 - wavefield decomposition
 - redatuming
 - inversion, e.g. stereo tomography

Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



Calibration of CRS attributes

- high sensitivity to inaccurate velocity
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- readily applicable to 3D data and deviated wells
- reliable geometrical CRS attributes for
 - wavefield decomposition
 - redatuming
 - inversion, e.g. stereo tomography
 - ▶ ...

Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



Calibration of CRS attributes

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 - wavefield decomposition
 - redatuming
 - inversion, e.g. stereo tomography

▶ ...

possible combination with hodogram analysis

Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



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- Paulsson Geophysical Services Inc. for providing synthetic data and tremendous assistance in questions of VSP imaging

Velocity calibration and wavefield decomposition

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Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition



Velocity calibration and wavefield decomposition

M. von Steht & J. Mann

Overview

Theory CRS stack for VSP FO CRS-Operator Calibration method

Data example Survey description Velocity calibration Decomposition

Conclusions & outlook



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